Introduction COMS10017 - Algorithms 1

Dr Christian Konrad







Algorithms?

A procedure that solves a *computational problem*



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A procedure that solves a computational problem

Computational Problem?

• How often does "Juliet" appear in Shakespeare's "Romeo And Juliet"?

A procedure that solves a computational problem

Computational Problem?

• How often does "Juliet" appear in Shakespeare's "Romeo And Juliet"? (181 times) (text/strings)

A procedure that solves a computational problem

- How often does "Juliet" appear in Shakespeare's "Romeo And Juliet"? (181 times) (text/strings)
- Sort an array of *n* numbers (all areas)

A procedure that solves a computational problem

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- Is it possible to partition the set {17, 8, 4, 22, 9, 28, 2} into two sets s.t. their sums are equal? (scheduling, load balancing)

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Brain Behind Your Software



Algorithms:

- Fabric that Software is made of
- Inner logic of your Software

Brain Behind Your Software



Algorithms:

- Fabric that Software is made of
- Inner logic of your Software
- \bullet Insufficient computational power \rightarrow Improve your algorithms!







• The faster the better: Time complexity





- The faster the better: **Time complexity**
- Use as little memory as possible: Space complexity





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Mathematics





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Mathematics

• We will prove that algorithms run fast and use little memory



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- We will prove that algorithms run fast and use little memory
- We will prove that algorithms are correct





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- Tools: Induction, algebra, sums, ..., rigorous arguments



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Theoretical Computer Science





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- Use as little memory as possible: Space complexity

Mathematics

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- We will prove that algorithms are correct
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Theoretical Computer Science

No implementations in this unit!





Algorithm 1 Single-pass Semi-Streaming Algorithm for MDS

Require: Bipartite input graph G = (A, B, E) with |A| = |B| = n

- 1: Let $D_1, D_2, \ldots, D_{\log n} \leftarrow \{\}$
- 2: For every $a \in A$: $d(a) \leftarrow 0$
- 3: $U \leftarrow \emptyset$ {Keep track of dominated nodes $(U \subseteq B \text{ always holds})$ }
- 4. For every $h \in B \cdot C(h) \leftarrow \pm \beta$ Output cover certificatel

Goals:



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Goals: First steps towards becoming an algorithms designer

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Goals: First steps towards becoming an algorithms designer

- Learn techniques that help you design & analyze algorithms
- Onderstand a set of well-known algorithms

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• Study a problem, discover structure within it, exploit structure and design algorithms

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- Useful in all areas of Computer Science

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Systematic Approach to Problem/Puzzle Solving

- Study a problem, discover structure within it, exploit structure and design algorithms
- Useful in all areas of Computer Science
- Interview Questions: Google, Facebook, Amazon, etc.

My Goals



My Goals

• Get you excited about Algorithms



My Goals

- Get you excited about Algorithms
- Shape next generation of Algorithm Designers at Bristol



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Algorithms in Bristol

• 1st year: Algorithms (Algorithms 1)



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Algorithms in Bristol

- 1st year: Algorithms (Algorithms 1)
- 2nd year: Algorithms 2

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Algorithms in Bristol

- 1st year: Algorithms (Algorithms 1)
- 2nd year: Algorithms 2
- 3rd year: Advanced Algorithms (Algorithms 3)

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Algorithms in Bristol

- 1st year: Algorithms (Algorithms 1)
- 2nd year: Algorithms 2
- 3rd year: Advanced Algorithms (Algorithms 3)
- 4th year: Advanced Topics in Theoretical Computer Science (Algorithms 4)

My Goals

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Algorithms in Bristol

- 1st year: Algorithms (Algorithms 1)
- 2nd year: Algorithms 2
- 3rd year: Advanced Algorithms (Algorithms 3)
- 4th year: Advanced Topics in Theoretical Computer Science (Algorithms 4)

BSc/MEng Projects, Reading Group, Summer Internships, PhD students

Teaching Sessions

- Lectures: Mondays 3pm, Thursdays 11pm
- **Problem sheet sessions:** (Tuesdays) TA-led problem sheet sessions, come prepared!
- **OPTIONAL Drop-in/discussion session:** (Mondays 10am-11am) ask questions about the material or other algorithms-related topics
- **OPTIONAL Office hours:** (Mondays 4pm-5pm) Ask me anything about the unit

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Assessment

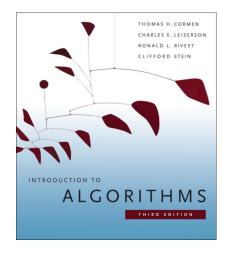
- Exam: Counts 50% towards your final mark in the joint unit "Object-Oriented Programming and Algorithms"
- $\bullet\,$ You pass the joint unit if your final grade is at least $40\%\,$

Teaching Staff

- Unit Director: Dr Christian Konrad (christian.konrad@bristol.ac.uk)
- Lead TA: Adithya Diddapur (adi.diddapur@bristol.ac.uk)

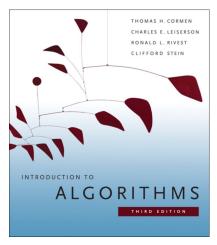


• **TAs:** Alexander Bell, Michael Degamo, Amos Holland, Piotr Kozicki, Philip Mortimer, Conor O'Sullivan, Thomas Parr, Robert Popescu, Jaehyun Roh, Thammadol Tansrivorarat, Archie Walton, Eric Wang



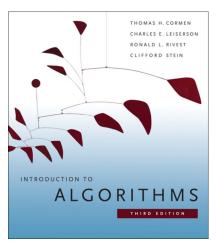


• More details on many of the topics discussed in this unit



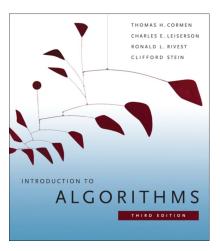


- More details on many of the topics discussed in this unit
- However, not all topics can be found in this book





- More details on many of the topics discussed in this unit
- However, not all topics can be found in this book
- Unit materials cover everything you need to know





• Make sure you understand the material

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- Work on provided exercises!

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- Use MS Teams channel for discussions and questions

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Unit webpage: Use link on blackboard

https://bristolalgo.github.io/courses/2023_2024_ COMS10017/coms10017.html

This Week

- Monday 3pm-4pm: Lecture (today)
- OPTIONAL Monday 4:15pm-5pm: Office hours (MVB03.06)
- Thursday 11am-12pm: Lecture

Next Week

- Monday 3pm-4pm: Lecture
- OPTIONAL Monday 4pm-5pm: Drop-in Session in 1.06QB (exception!)
- Tuesday: Small-group problem sheet sessions
- Thursday 11am-12pm: Lecture

Every Subsequent Week

- OPTIONAL Monday 10am-11am: Drop-in Session in 1.60QB
- Monday 3pm-4pm: Lecture
- OPTIONAL Monday 4:15pm-5pm: Office Hours
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Good luck and enjoy! Questions?